

**P7.3-2**

$$i(t) = C \frac{d}{dt} v(t) = \frac{1}{8} \frac{d}{dt} 12 \cos(2t + 30^\circ) = \frac{1}{8} (12)(-2) \sin(2t + 30^\circ) = 3 \cos(2t + 120^\circ) \text{ A}$$

**P7.3-4**

$$v(t) = \frac{1}{C} \int_0^t i(\tau) d\tau + v(0) = \frac{1}{2 \times 10^{-12}} \int_0^t i(\tau) d\tau - 10^{-3}$$

$$0 < t < 2 \times 10^{-9} \quad i_s(t) = 0 \Rightarrow v(t) = \frac{1}{2 \times 10^{-12}} \int_0^t 0 d\tau - 10^{-3} = -10^{-3}$$

$$2 \times 10^{-9} < t < 3 \times 10^{-9} \quad i_s(t) = 4 \times 10^{-6} \text{ A}$$

$$\Rightarrow v(t) = \frac{1}{2 \times 10^{-12}} \int_{2\text{ns}}^t (4 \times 10^{-6}) d\tau - 10^{-3} = -5 \times 10^{-3} + (2 \times 10^6) t$$

$$\text{In particular, } v(3 \times 10^{-9}) = -5 \times 10^{-3} + (2 \times 10^6)(3 \times 10^{-9}) = 10^{-3}$$

$$3 \times 10^{-9} < t < 5 \times 10^{-9} \quad i_s(t) = -2 \times 10^{-6} \text{ A}$$

$$\Rightarrow v(t) = \frac{1}{2 \times 10^{-12}} \int_{3\text{ns}}^t (-2 \times 10^{-6}) d\tau + 10^{-3} = 4 \times 10^{-3} - (10^6) t$$

$$\text{In particular, } v(5 \times 10^{-9}) = 4 \times 10^{-3} - (10^6)(5 \times 10^{-9}) = -10^{-3} \text{ V}$$

$$5 \times 10^{-9} < t \quad i_s(t) = 0 \Rightarrow v(t) = \frac{1}{2 \times 10^{-12}} \int_{5\text{ns}}^t 0 d\tau - 10^{-3} = -10^{-3} \text{ V}$$

**P7.4-2**

$$i_c = C \frac{dv}{dt} = (10 \times 10^{-6})(-5)(-4000)e^{-4000t} = \underline{0.2e^{-4000t} \text{ A}} \Rightarrow \begin{cases} i_c(0) = 0.2 \text{ A} \\ i_c(10\text{ms}) = 8.5 \times 10^{-10} \text{ A} \end{cases}$$

$$\mathcal{W}(t) = \frac{1}{2} C v^2(t) \quad \text{and} \quad v(0) = 5 - 5e^0 = 0 \Rightarrow \underline{\mathcal{W}(0) = 0}$$

$$v(10 \times 10^{-3}) = 5 - 5e^{-40} = 5 - 21.2 \times 10^{-18} \cong 5 \Rightarrow \underline{\mathcal{W}(10) = 1.25 \times 10^{-4} \text{ J}}$$

**P7.5-1**

$$2 \mu\text{F} \parallel 4 \mu\text{F} = 6 \mu\text{F}$$

$$6 \mu\text{F} \text{ in series with } 3 \mu\text{F} = \frac{6 \mu\text{F} \cdot 3 \mu\text{F}}{6 \mu\text{F} + 3 \mu\text{F}} = 2 \mu\text{F}$$

$$i(t) = 2 \mu\text{F} \frac{d}{dt} (6 \cos 100t) = (2 \times 10^{-6})(6)(100)(-\sin 100t) \text{ A} = \underline{-1.2 \sin 100t \text{ mA}}$$

**P7.5-3**

$$C \text{ in series with } C = \frac{C \cdot C}{C + C} = \frac{C}{2}$$

$$C \parallel C \parallel \frac{C}{2} = \frac{5}{2}C$$

$$C \text{ in series with } \frac{5}{2}C = \frac{C \cdot \frac{5}{2}C}{C + \frac{5}{2}C} = \frac{5}{7}C$$

$$(25 \times 10^{-3}) \cos 250t = \left(\frac{5}{7}C\right) \frac{d}{dt}(14 \sin 250t) = \left(\frac{5}{7}C\right)(14)(250) \cos 250t$$

$$\text{so } 25 \times 10^{-3} = 2500 C \Rightarrow C = 10 \times 10^{-6} = 10 \mu\text{F}$$

**P7.6-4**

$$\begin{aligned} v(t) &= (250 \times 10^{-3}) \frac{d}{dt} (120 \times 10^{-3}) \sin(500t - 30^\circ) = (0.25)(0.12)(500) \cos(500t - 30^\circ) \\ &= 15 \cos(500t - 30^\circ) \end{aligned}$$

**P7.6-5**

$$i_L(t) = \frac{1}{5 \times 10^{-3}} \int_0^t v_s(\tau) d\tau - 2 \times 10^{-6}$$

$$\text{for } 0 < t < 1 \mu\text{s} \quad v_s(t) = 4 \text{ mV}$$

$$i_L(t) = \frac{1}{5 \times 10^{-3}} \int_0^t 4 \times 10^{-3} d\tau - 2 \times 10^{-6} = \left(\frac{4 \times 10^{-3}}{5 \times 10^{-3}}\right)t - 2 \times 10^{-6} = 0.8t - 2 \times 10^{-6} \text{ A}$$

$$i_L(1 \mu\text{s}) = \left(\frac{4 \times 10^{-3}}{5 \times 10^{-3}}(1 \times 10^{-6})\right) - 2 \times 10^{-6} = -\frac{6}{5} \times 10^{-6} \text{ A} = -1.2 \mu\text{A}$$

$$\text{for } 1 \mu\text{s} < t < 3 \mu\text{s} \quad v_s(t) = -1 \text{ mV}$$

$$i_L(t) = \frac{1}{5 \times 10^{-3}} \int_{1 \mu\text{s}}^t (-1 \times 10^{-3}) d\tau - \frac{6}{5} \times 10^{-6} = -\frac{1 \times 10^{-3}}{5 \times 10^{-3}}(t - 1 \times 10^{-6}) - \frac{6}{5} \times 10^{-6} = (-0.2t - 10^{-6}) \text{ A}$$

$$i_L(3 \mu\text{s}) = \left(-\frac{1 \times 10^{-3}}{5 \times 10^{-3}} + 3 \times 10^{-6}\right) - 1 \times 10^{-6} = -1.6 \mu\text{A}$$

$$\text{for } 3 \mu\text{s} < t \quad v_s(t) = 0 \text{ so } i_L(t) \text{ remains } -1.6 \mu\text{A}$$

**P7.7-2**

$$\begin{aligned}
 p(t) &= v(t) i(t) = \left[ 5 \frac{d}{dt} (4 \sin 2t) \right] (4 \sin 2t) \\
 &= 5 (8 \cos 2t) (4 \sin 2t) \\
 &= 80 [2 \cos 2t \sin 2t] \\
 &= 80 [\sin(2t+2t) + \sin(2t-2t)] = 80 \sin 4t \text{ W} \\
 w(t) &= \int_0^t p(\tau) d\tau = 80 \int_0^t \sin 4\tau d\tau = -\frac{80}{4} [\cos 4\tau]_0^t = 20 (1 - \cos 4t)
 \end{aligned}$$

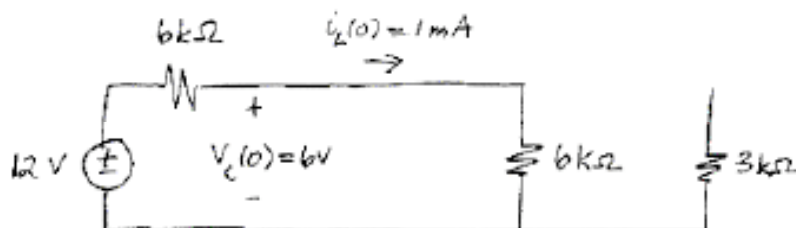
**P7.8-2**

$$4 \text{ mH} + 4 \text{ mH} = 8 \text{ mH} \quad , \quad 8 \text{ mH} \parallel 8 \text{ mH} = \frac{(8 \times 10^{-3}) \times (8 \times 10^{-3})}{8 \times 10^{-3} + 8 \times 10^{-3}} = 4 \text{ mH}$$

and  $4 \text{ mH} + 4 \text{ mH} = 8 \text{ mH}$

$$v(t) = (8 \times 10^{-3}) \frac{d}{dt} (5 + 3e^{-250t}) = (8 \times 10^{-3})(0 + 3(-250)e^{-250t}) = -6 e^{-250t} \text{ V}$$

**P7.9-2**



Then

$$i_L(0^+) = i_L(0^-) = 1 \text{ mA} \quad \text{and} \quad v_C(0^+) = v_C(0^-) = 6 \text{ V}$$

Next

