

(1)

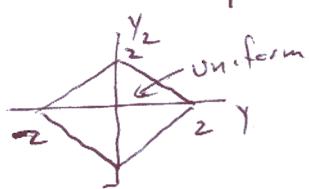
$$a \quad p(x_1, x_2) = p(x_1)p(x_2) \quad \text{Note } p(x_1) = \int p(x_1, x_2) dx_2 \quad \text{for all } x_1$$

Note: This is Hadamard transform

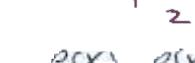
$$p(x_2) = \int p(x_1, x_2) dx_1 + \text{for all } x_2$$

$$\Rightarrow p(x_1)p(x_2) = p(x_1) \text{ for } x_2$$

$$b \quad p(y_1, y_2) = f_x \underbrace{\frac{y_1+y_2}{2}}_{\frac{1}{4}} y_2 J \frac{1}{8} \quad \text{for all } y$$



uniform

$p(y_1)$ 
 $p(y_2)$ 
 $p(x_1) p(x_2)$ 

$\left. \begin{array}{l} p(x_1) * p(x_2) \\ \text{since } x_1 \text{ independent} \\ \text{and } y_1 = x_1 + x_2 \end{array} \right\}$

$A \quad y_1, y_2 \text{ independent} \quad p(y_1) = p(y_1) p(y_2)$
 \Rightarrow at point x_1 $\left. \begin{array}{l} p(y_1) * y_2 \\ \frac{1}{8} \end{array} \right\} = \frac{1}{4}$
 $p(y_1) * p(y_2) = p(y_1 + y_2) = p(y) = p(y_1) p(y_2)$

(2)

$$\phi_{xx}(t, \tau) = E \left\{ [A g(t) \cos(\pi f_1 t) + B g(t) \cos(2\pi f_2 t)] \right. \\ \left. [A g(t+\tau) \cos(f_1(t+\tau)) + B g(t+\tau) \cos(f_2(t+\tau))] \right\}$$

$$E[A^2] g(t) g(t+\tau) \cos(2\pi f_1 t) \cos(2\pi f_1(t+\tau))$$

$$E[B^2] g(t) g(t+\tau) \cos(2\pi f_2 t) \cos(2\pi f_2(t+\tau))$$

$$+ E[A B] g(t) g(t+\tau) \cos(2\pi f_1 t) \cos(2\pi f_2(t+\tau))$$

$$E[B A] g(t) g(t+\tau) \cos(2\pi f_2 t) \cos(2\pi f_1(t+\tau))$$

depends
 t, τ

simplify If A, B independent $E[A^2] g(t) g(t+\tau) \cos(2\pi f_1 t) \cos(2\pi f_1(t+\tau))$

$$\phi_{xx}(t, \tau) = E[A^2] g(t) g(t+\tau) \left[\cos(2\pi f_1 t) \cos(2\pi f_1(t+\tau)) \right] = f_1 \delta(t-\tau)$$

$$\frac{1}{2} E[B^2] g(t) g(t+\tau) \left[\cos(2\pi f_2 t) \cos(2\pi f_2(t+\tau)) \right]$$

(1) note $g(t) g(t+\tau) \rightarrow$ for $t = T$ $\delta(T-t)$



(2) \Rightarrow $f_1 \delta(t) + f_2 \delta(t) = f(t)$ but periodic in t

$$a) \int_{T/4}^{3T/4} \psi_1(t) \Rightarrow B = \sqrt{2}$$

$$\int_{T/4}^T \psi_1(t) dt \Rightarrow A = \frac{\sqrt{2}}{T}$$

$$b) \int_{T/4}^T \psi_1(t) \psi_2(t) dt = 0$$

$\psi_1(t) \psi_2$

$$S_i \quad \psi_1(t) + \psi_2(t)$$

$$S_i(t) = \psi_1(t) + \psi_2(t)$$

$$S_i(t)$$

$E(t)$ is stationary

$A \quad B$